# Shape Control in Gold Nanoparticles by N-Containing Ligands: Insights from Density Functional Theory and Wulff Constructions

M. Domingo<sup>1</sup> · M. Shahrokhi<sup>1</sup> · I. N. Remediakis<sup>2,3</sup> · N. Lopez<sup>1</sup>

#### **Abstract**

The controlled growth promoted by the use of ligands can affect the structural properties of nanoparticles, preferential growth and most likely exposed facets in their final shape. The chemistry is deeply dominated by the close relationship between both the interaction of the ligands and the metal structure. In the present work, we have illustrated the change in the nanoparticle shape as a function of a series of nitrogen bases. Particularly, we have employed Density Functional Theory to obtain the interaction energies of a series of nitrogen containing bases to gold surfaces with different orientations. The adsorption strength is found to correlate with the HOMO position of the ligand thus providing a fast screening tool for this property. Moreover, for small N-bases with high N content we have found that the shape can be tuned as a function of the coverage and the final structure at high coverages severely departs from that of bare gold nanoparticles. We have found variations in the different extension of the facets that can be further employed in obtaining structure sensitivity and the right chemical and catalytic performance.

**Keywords** Gold nanoparticles · N-containing ligands · Density Functional Theory (DFT) · Wulff construction

## 1 Introduction

Gold chemistry has intrigued scientists in both homogeneous and heterogeneous catalysis for more than two decades now [1–4]. Particularly, when prepared highly porous, the catalytic activity is more prominent likely due to the presence of a larger fraction of low coordinated sites [5–8]. Most of the mechanisms for the reactivity on clean metals or organometallic compounds have been clarified [9] but there is still a wide open area regarding ligand coated nanoparticles that might abridge the properties between the two materials.

Among the most likely properties, ligand-induced shape control is the most obvious. Colloidal chemistry has a rich toolbox that allows the synthesis of different nanoarchitectures by changing the nature of the ligands. However, the intimate mechanisms that apply are not known in a large detail in part because of the multiscale nature of the problem of nucleation and growth [10]. A very successful approach however is the use of Density Functional Theory, DFT, to understand the very fundamental modifications induced at the atomistic scale by the adsorption of ligands. Indeed, employing traditional methodologies based on a continuum model that allows the calculation of the surface energy via DFT and its combination with ab-initio thermodynamics has proven a useful tool when assessing the tridimensional structure of nanoparticles [11–14] for a large variety of systems and including concave nanoparticles [15]. As reactions are often differently promoted by facet orientation (structure sensitivity) the shape control of the nanocatalyst is of primarily interest.

Among all ligands N-containing ones have emerged as the most suitable for further co-catalytic activity [16]. The reason behind the activity of these N-bases as ligands can be traced back to the fact that when adsorbed on a metal surface they form frustrated Lewis pairs (FLP) [17, 18] that allow the easy activation of H<sub>2</sub> otherwise impossible for bulk Au. This concept has been recently reviewed [19]. Therefore, the study of the interaction of a series of N-bases on different

Institute of Chemical Research of Catalonia, ICIQ, The Barcelona Institute of Science and Technology, Av. Països Catalans 16, 43007 Tarragona, Spain

Department of Materials Science and Technology, University of Crete, Heraklion, Greece

<sup>&</sup>lt;sup>3</sup> Institute of Electronic Structure and Laser, FORTH, Heraklion, Greece

facets of gold is mandatory to identify if the presence of these ligands affects also the overall shape of the gold nanoparticles thus adding to the electronic contribution of the FLP a modulation different facets in the metal nanoparticles.

In the present work, we have taken a list of the most common N-bases with different hapticity to evaluate the effects of the ligands on the exhibited surfaces. The molecules are: aniline, ethylenediamine, pyrazine, pyridine, pyrrole, trimethylamine and porphine, see Scheme 1. By means of Density Functional Theory we have computed the adsorption of these ligands to the low-Miller-index facets of gold. The ligand-decorated surface energies have then been employed in the Wulff and atomistic Wulff construction to derive the equilibrium shape of the corresponding gold nanoparticles.

## 2 Computational Details

We have performed Density Functional Theory calculations using the Vienna ab initio simulation package code (VASP) [20, 21] with the Perdew–Burke–Enzerhof (PBE) exchange–correlation functional [22]. The interaction between the valence and the core electrons was described with the projected augmented wave (PAW) method with the implementation of Kresse and Joubert [23]. The energy cutoff was set to 450 eV and van der Waals contributions were described using the semi-empirical DFT-D2 approach [24, 25] and the parameters were reoptimized for this metal in our group [26]. The calculations of surface energy were carried out for various terminations of three low-index planes: (001), (110) and (111) using periodic boundary conditions. The models for (100) and (111) Au surface were constructed with five atomic

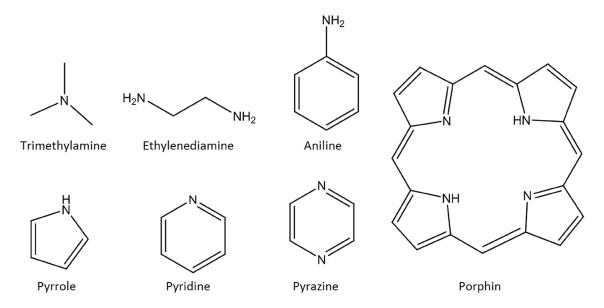
layers while (110) was modeled with 9 atomic layers where the two topmost layers were fully relaxed and the others were fixed to their bulk positions. To ensure the decoupling of the adjacent slabs, a 12 Å thick vacuum region was employed for all slabs. The N-ligands were adsorbed on the topmost layer and dipole correction was used. For all ligand molecules adsorption except porphine, the (100), (110) and (111) Au surfaces were modeled by a slab consisting of a  $4\times4$ ,  $3\times3$ , and  $4\times4$ surface unit cell, respectively, and were optimized using a  $(3\times3\times1)$ ,  $(2\times3\times1)$ , and  $(3\times3\times1)$  k-point mesh. For porphine adsorption, a slab model consisting  $5 \times 5$ ,  $4 \times 5$  and  $5 \times 5$ surface unit cell were used for the (100), (110) and (111) facets and optimized using a  $(3\times3\times1)$ ,  $(2\times3\times1)$ , and  $(3\times3\times1)$ k-point mesh, respectively. All the computed structures have been incorporated to the ioChem-BD database [27] and can be retrieved through the following https://doi.org/10.19061/ iochem-bd-1-49.

### 3 Results

In this paper, we discuss the characteristics of each Au surface and the adsorption behavior of different ligands on all of them. We begin by calculating the surface energy,  $\gamma_s$ , for Au by simulations of periodic slabs. For a given model slab of a facet featuring Miller index (hkl), the  $\gamma_s$  is given by the following expression:

$$\gamma_{s} = \frac{1}{2A} \left[ E_{slab}^{unrelax} - N E_{bulk} \right] + \frac{1}{A} \left[ E_{slab}^{relax} - E_{slab}^{unrelax} \right] \tag{1}$$

where A is area of the surface considered,  $E_{slab}^{unrelax}$  and  $E_{slab}^{relax}$  are the respective total energies of the unrelaxed and relaxed N-atom slabs, N is the number of atoms in the slab,



Scheme 1 N-bases employed in the present study. The molecules differ on the hapticity, dispersion contributions and extension

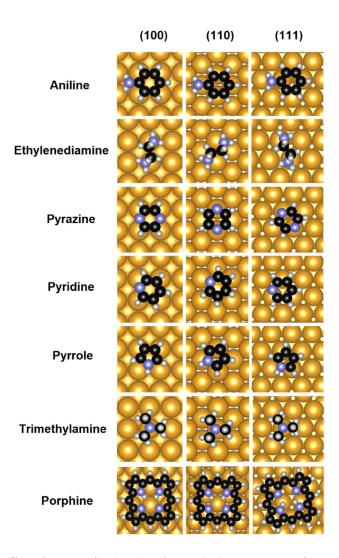
and  $E_{bulk}$  the total energy of Au bulk per atom, and the factor 1/2 accounts for the two surfaces in the slab unit-cell in an asymmetric configuration, relaxation taking place only on one the sides. The results, listed in Table 1, showed that (111) facet is most stable with a surface energy of  $0.057 \, {\rm eV/ \, \mathring{A}^2}$ . Our results are in reasonable agreement with the tests performed by Marzari [28]. We have also calculated the energy penalty to remove one atom from the lattice placing it as an adatom for (100), (110) and (111) facets and are 0.60, 1.00 and  $1.20 \, {\rm eV}$ . Therefore, the energy gain by adsorbing the ligand on the adatom with respect to the regular position needs to be larger than these thresholds to set a thermodynamic force for reconstruction.

Adsorption was only allowed on one of the sides of the Au slabs. We begin by calculating the adsorption energy for several different adsorption sites of the planar (100), (110), and (111) surfaces to ensure that the global minimum is found. The adsorption energies of the Ligand molecules were calculated with respect to the solution as follows:

$$E_{ads} = (E_{S\text{-}Ligand} - E_S - E_{Ligand}^{gas\text{-}phase}) \tag{2}$$

where  $E_{S\text{-}Ligand}$  is the energy of the surface with the ligand molecule,  $E_S$  is the energy of the simulation cell containing the surface only, and  $E_{Ligand}^{gas\text{-}phase}$  is the energy of the molecule

in the gas phase, calculated using the same conditions. Figure 1 shows the structure of the Ligand/Au systems after relaxation. It is revealed that the bridge and on-top adsorption sites for all molecules are the most stable ones with exothermic adsorption energies and that hollow sites are highly unfavorable. The adsorption energies for the adsorption of ligand molecules on different facets of Au surfaces reported in Table 1. The largest value for the adsorption energy ( $E_{ads}$ ) per molecule is that for the Au(110) surface. Moreover, porphine has the strongest interaction with Au surfaces among all molecules. The average distances between C and N atoms of ligand and the first layer of Au



**Fig. 1** Structures for the adsorption on the lowest energy surfaces. Color code: orange surface Au atoms, black C atoms, purple N atoms and gray H atoms

Table 1 Hapticity and adsorption energies,  $E_{ads}$  in eV, for the different ligands in this study on different Au surfaces

Ligand	Hapticity			E <sub>ads</sub>			γ΄		
	(111)	(100)	(110)	(111)	(100)	(110)	(111)	(100)	(110)
None							0.057	0.064	0.066
Aniline	4	4	2	-0.553	-0.569	-0.992	0.048	0.056	0.049
Ethylenediamine	2	2	2	-0.797	-0.927	- 1.312	0.037	0.044	0.032
Pyrazine	4	4	2	-0.230	-0.204	-0.543	0.053	0.061	0.061
Pyridine	3	4	2	-0.289	-0.262	-0.301	0.052	0.060	0.057
Pyrrole	3	4	2	-0.470	-0.454	-0.807	0.049	0.057	0.052
Trimethylamine	1	1	1	-0.607	-0.615	-0.903	0.047	0.055	0.050
Porphine	9	9	9	- 1.49	- 1.55	- 2.10	0.049	0.056	0.058

Adsorption corrected surface energies,  $\gamma'$  in  $eV/\mathring{A}^2$ , for the different molecules in this study on different Au surfaces

slab are presented in Table 2. It can be seen that the smallest distance between ligands and Au surface is that for (110) facet which lead to the largest value of  $E_{ads}$ . The gas-phase adsorption energies are used in Table 1, when the relevant experiments may be done in the liquid phase. To probe the effects of solvation on adsorption energies of ligands on Au surface we applied recently developed a continuum solvation model into the VASP, a plane-wave based electronic structure code, VASP-MGCM (VASP-Multigrid Continuum Model) [29]. Water solvation of ethylene diamine is exothermic by 0.27 eV. Therefore, the binding energies reported for this ligand in Table 1 would be reduced to -0.6 for the (111) surface and about -1.1 eV for (110).

To further discern the interaction between ligands and Au surface charge density difference between pyrazine (weak interaction), aniline (moderate interaction) and ethylenediamine (strong interaction) ligands and different facets of Au slab has been calculated and illustrated in Fig. 2. It can be seen that electrons are accumulated under the vacuum region and the middle part between the ligands and the Au atoms. The accumulation of more electrons in the middle part creates the stronger interactions between the ligands and the Au surface. The pyrazine has a weak interaction on all Au facets

leading to small influence on gold nanoparticle shape while the ethylenediamine has a big influence on the shape of nanoparticle due to strong interaction with Au surfaces. The interaction between aniline and (110) facet is strong unlike (100) and (111) facets hence it has a bigger influence on (110) facet than other ones. In order to analyze the effect of each ligand on gold nanoparticle shape the adsorption corrected surface energies are calculated.

To rationalize the strength of the bond at the interface we have looked at the trends behind adsorption. Particularly, the basicity of the ligand controls the adsorption. In particular, we have plotted the normalized (per free N atom) E<sub>ads</sub>/N as a function of the HOMO position of the ligands, see Fig. 3. The strongest interactions always correspond to the (110) surface. For all surfaces, a linear dependence is found, showing the predominant role of the basicity of the ligand in the adsorption.

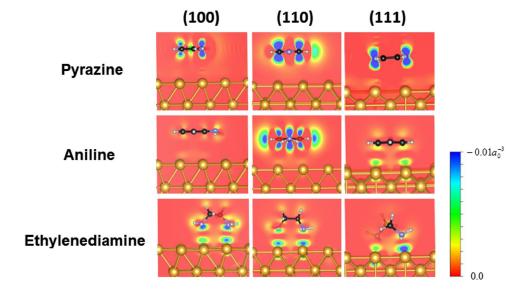
When the Au nanoparticle interacts with the surrounding environment, the surface energy is replaced by the adsorption corrected surface energies (interface tensions),  $\gamma'$ , between Au and its environment which at T=0 K is given by

$$\gamma' = \gamma_s + \frac{fE_{ads}}{A} \tag{3}$$

Table 2 Average distance between N or C atoms of the ligands and the topmost Au surface in Å

Ligand	(111)		(100)		(110)	
	N	С	N	С	N	С
Aniline	3.59	3.54	3.50	3.44	2.83	2.66
Ethylenediamine	2.57	3.67	2.60	3.74	2.04	2.35
Pyrazine	3.96	3.96	4.03	4.03	3.35	3.41
Pyridine	3.81	3.82	3.84	3.87	2.32	3.06
Pyrrole	3.42	3.42	3.41	3.42	2.72	2.62
Trimethylamine	2.98	3.43	2.98	3.42	2.48	2.89
Porphine	3.33	3.33	3.02	3.05	2.52	2.60

Fig. 2 Cross-sectional views of the charge density difference for pyrazine, aniline and ethylenediamine on different facets of Au surface for negative charge carriers ( $a_0$ : Bohr radius). Color code: like Fig. 1



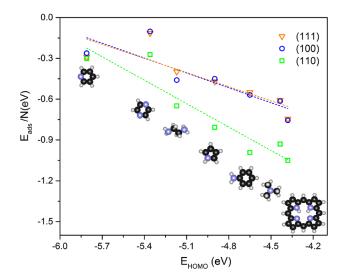


Fig. 3 Normalized (per free N atom)  $E_{ads}\!/N$  as a function of the HOMO position of the ligands

where f is the area of each surface facet to the minimum area required for ligands adsorption on the Au surfaces  $f = \frac{S_{cell}}{S_{mol}}$  assuming that the molecules lay flat. This is an

approximation as at very high coverages the molecules could be adsorbed through the N atoms leaving the pi-systems interacting out of the surface; however this assumption simplifies the discussion and is relevant in a certain ligand concentration regime close to saturation. In our calculations we used f = 2 for all ligand molecules adsorption except

ethylenediamine and porphine for which values of 3 and 1 were used, respectively. The adsorption corrected surface energies for all molecules and different Au facets are listed in Table 1. It can be seen that the (111) facet is still the most stable surface after adsorbing molecules and other (hkl) planes have much higher surface energies. The equilibrium morphology of the nanoparticles was obtained through the Wulff construction method [30] which depends on the relative  $\gamma'$  from Table 1. Figure 4 illustrates the Wulff structures for bare Au nanoparticle and ligand-covered Au system. The crystal morphology model was created with VESTA (Visualization for Electronic and Structural Analysis) version 3.4.0 package [31]. We also calculated total volume and fraction of each of the surfaces as a function of ligand for a nanoparticle with a radius of 5 nm (Table 3). The total volume for bare Au nanoparticle is 73.42 nm<sup>3</sup> where the dominant facet is (111) surface with the fraction surface value of 0.65, in good agreement with previous works [4, 13, 28, 32]. From Fig. 4 and Table 3, it can be concluded that for all molecules adsorption except aniline and ethylenediamine the dominant facet is still (111) while for two latest ligands, nanoparticle surface is dominated by (110) facet. In addition, the pyrazine, pyridine and porphine molecules have a very small influence on Au nanoparticle morphology after adsorption while aniline, ethylenediamine, pyrrole and trimethylamine completely change the morphology of Au nanoparticle. For the latest molecules the fraction of (110) facet increases in comparison with bare Au nanoparticle while regions of (111) facet decrease. Regions for (100) facet is almost same for the pyrazine, pyridine and porphine

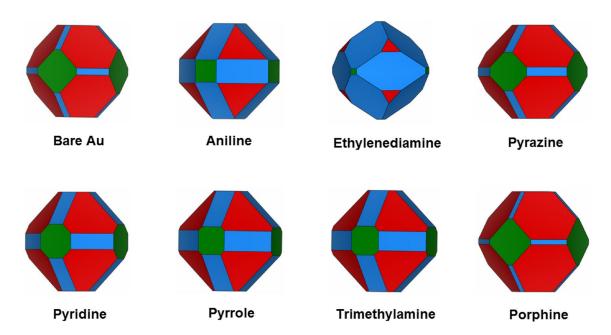


Fig. 4 Wulff constructions for gold decorated nanoparticles as a function of the adsorbate: red planes are (111), green planes are (100) and blue planes are (110) facets

**Table 3** Total volume, fraction of each of the surfaces as a function of ligand for a nanoparticle with a diameter of 5 nm

Ligand	Volume (nm <sup>3</sup> )	(111)	(100)	(110)
Bare Au	73.42	0.65	0.25	0.10
Aniline	72.59	0.31	0.12	0.57
Ethylenediamine	57.20	0.05	0.01	0.94
Pyrazine	73.42	0.63	0.22	0.15
Pyridine	73.42	0.52	0.19	0.29
Pyrrole	69.96	0.43	0.15	0.42
Trimethylamine	69.96	0.46	0.16	0.38
Porphine	74.90	0.70	0.23	0.07

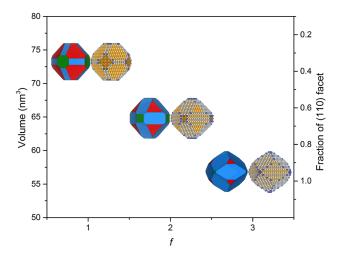


Fig. 5 Wulff and atomistic Wulff constructions for ethylenediamine-covered Au system at different coverages. Color code as in Fig. 4

molecules after adsorption while it is decreased in other ones.

To show the effect of molecular coverage on the Au nanoparticle shape, both the continuous and the atomistic Wulff structure of ethylenediamine-covered Au system at different coverages is plotted versus nanoparticle volume (and fraction of (110) facet) in Fig. 5. As it can be seen by increasing ethylenediamine coverage the fraction of (110) facet increases while nanoparticle volume and regions of (111) and (100) facets decrease. The total volume for ethylenediamine-covered Au nanoparticle is 73.42, 65.37 and 57.20 nm<sup>3</sup> for f = 1, 2 and 3, respectively. The related values of the fraction of (110) facet is 31, 70 and 94% for same coverages. Similarly from the atomistic Wulff construction the number of low coordinated atoms can be retrieved. For the lowest coverage the fraction of low coordinated (NC=3) atoms is 1.2% and NC = 5 is about 5%. Instead at higher ligand content these two fractions raise to 1.7 and 13%. Finally, for the highest ethylene diamine content the fraction of these atoms are 2.1 and 15%, respectively.

In summary, the adsorption of N-bases can modify significantly the shape of nanoparticles increasing facets that are not expressed in clean gold nanoparticles. This will modify the catalytic properties in two directions as electron modifiers and for reactions with structure sensitivity as a different facet is present is the most common one in ethylenediamine.

#### 4 Conclusions

We have constructed and characterized gold nanoparticle morphology in thermodynamic equilibrium, including interactions with 7 different ligand molecules (aniline, ethylenediamine, pyrazine, pyridine, pyrrole, trimethylamine and porphine) using the Wulff construction. We first studied low-index Au surfaces [(100), (110) and (111)], both clean and with ligand molecules adsorbed on them. We found that the bridge and on-top adsorption sites for all molecules are the most stable ones with exothermic adsorption energies. Adsorption is found to correlate with the number of N atoms in contact with the surface and the HOMO (donor) ability of the ligand.

The adsorption of pyrazine, pyridine and porphine molecules does not change the Au nanoparticle morphology while the adsorption of aniline, ethylene diamine, pyrrole and trimethylamine increases regions of (110) facet and decreases regions of (111) facet, leading a major change in Au nanoparticle morphology. Particularly for ethylene diamine the change of the shape with concentration illustrates the important role of small ligands in the final shape of nanoparticles. As both the nature of the ligands and the induced shape changes might affect adsorption and reaction on nanoparticles a full design of the interface will be required to fully benefit from the synergetic effects at the interface.

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